



# The Value of Observations in Determination of Optimal Vaccination Timing and Threshold

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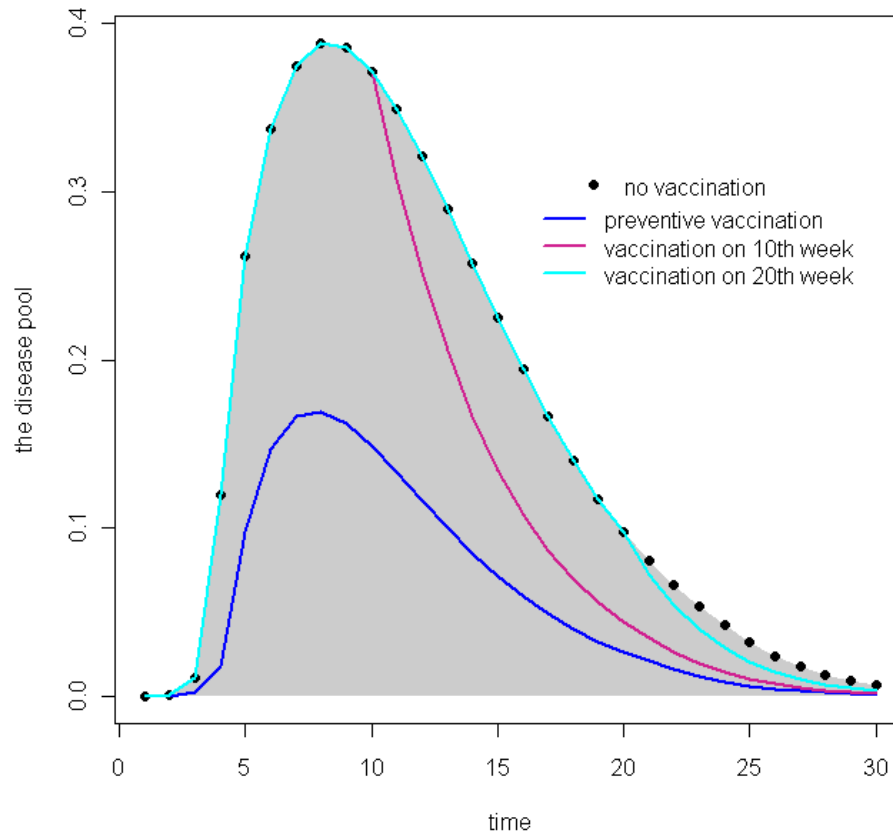


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# GEO-BENE

- **Global Earth Observation – Benefit Estimation: Now, Next and Emerging.**
  - » [www.geo-bene.eu](http://www.geo-bene.eu)
- **Objective:** To develop methodologies and analytical tools to assess economic, social & environmental effects of improved quantitative and qualitative information delivered by GEOSS for the **nine** benefit areas of GEO.
- The benefit areas include *health*, *climate* and *weather*.

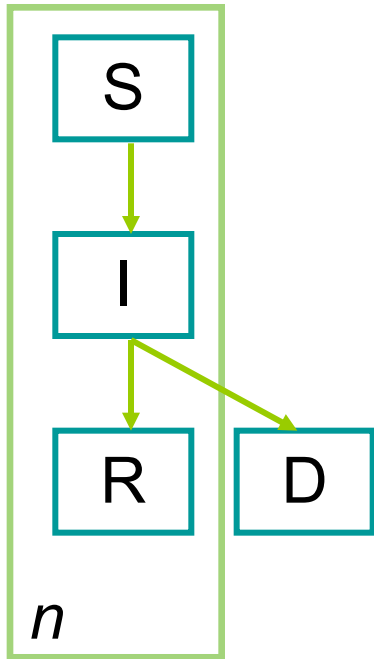
# Dynamics of an epidemic



# Meningococcal Meningitis

- In sub-Saharan Africa, infectious and parasitic diseases (excluding HIV/AIDS and including respiratory infections) were responsible for over 200 disease-adjusted life years per 1000 population. (Lancet, 1997)
- A polysaccharide vaccine for meningitis is available. New vaccine is being tested.
- Association of meningitis epidemics with dust storms (Science, 2008) and other environmental factors (Emerg Infect Dis 2003) has been suggested.

# Susceptible-Infected-Recovered (SIR) Model



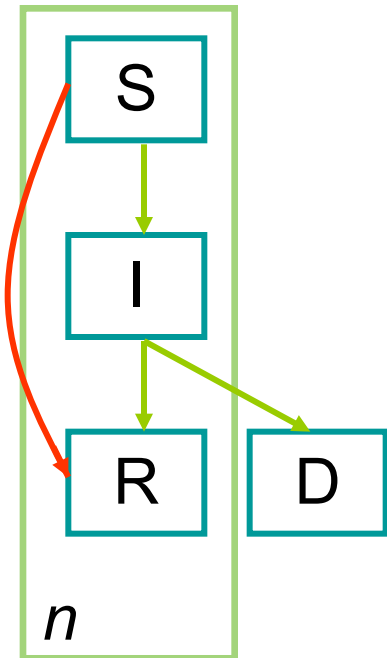
$$S(t) = S(t-1) - I.\text{new}(t-1)$$

$$I(t) = I(t-1) + I.\text{new}(t-1) - D.\text{new}(t-1) - R.\text{new}(t-1)$$

$$R(t) = R(t-1) + R.\text{new}(t-1)$$

$$n(t) = n(t-1) - D.\text{new}(t-1)$$

# Susceptible-Infected-Recovered (SIR) Model



$$S(t) = S(t-1) - I.\text{new}(t-1) - u(t)\alpha S(t-1)$$

$$I(t) = I(t-1) + I.\text{new}(t-1) - D.\text{new}(t-1) - R.\text{new}(t-1)$$

$$R(t) = R(t-1) + R.\text{new}(t-1) + u(t)\alpha S(t-1)$$

$$n(t) = n(t-1) - D.\text{new}(t-1)$$

# Susceptible – Infected – Recovered (SIR) Model

- Probability of becoming infected:

$$p(t) = 1 - \left( 1 - \frac{\pi(t)I(t)}{n(t) - 1} \right)^N$$

- Dynamics:

$$I.\text{new}(t) \sim \text{Bin}(S(t), p(t))$$

$$\{R.\text{new}(t), D.\text{new}(t), I(t) - R.\text{new}(t) - D.\text{new}(t)\} \sim \\ \text{Multinomial}(I(t), \{\gamma, \mu, 1 - \gamma - \mu\})$$

# Optimization:

$$\sum_{t=0}^T \frac{1}{(1 + \rho)^t} \{ u(t) c^{\text{vacc}} \alpha S(t) + c^{\text{treat}} I(t) + c^{\text{dead}} D.\text{new}(t) + c^{\text{seq}} \delta R.\text{new}(t) \}$$

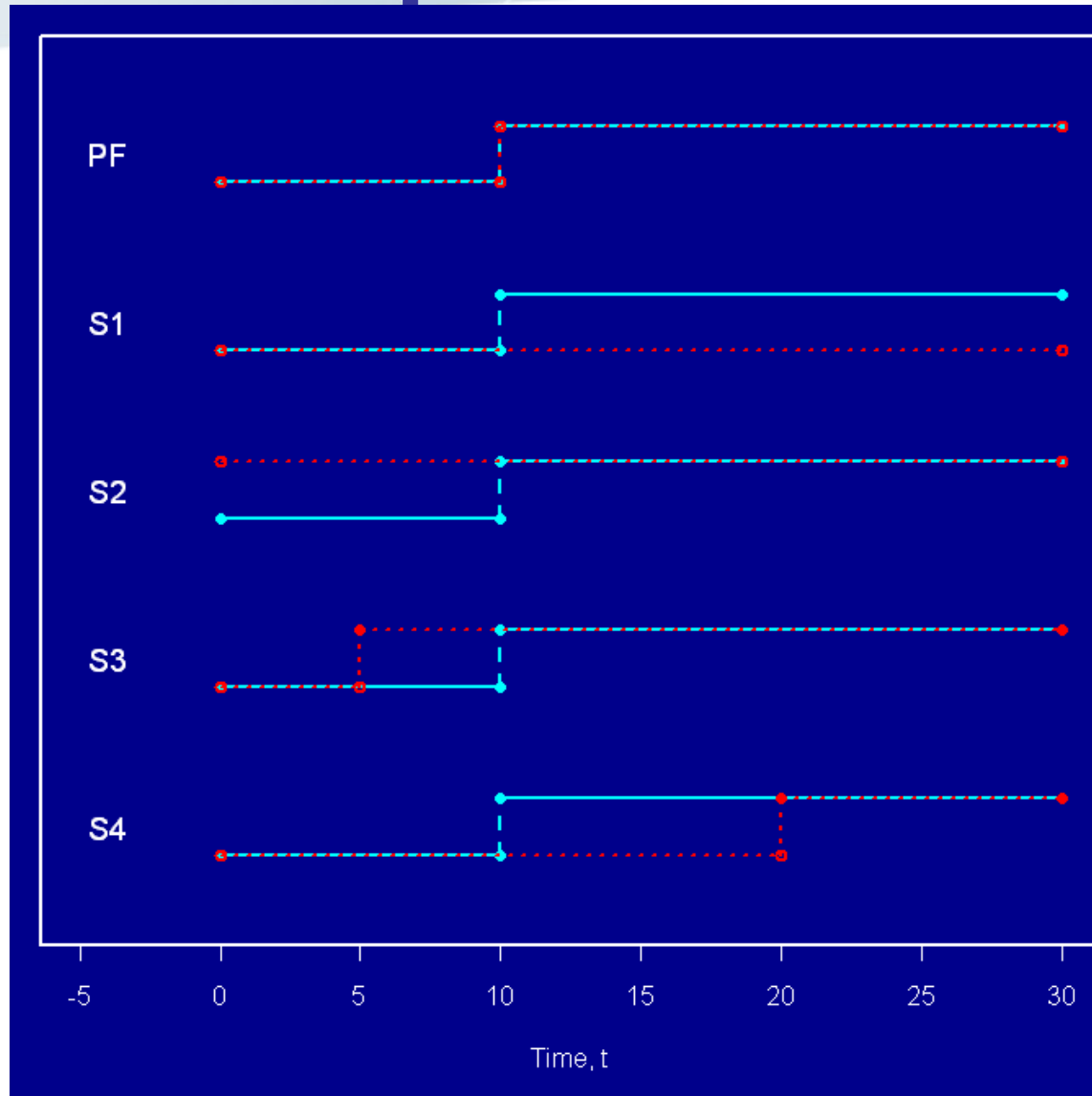
- cost of vaccination
- cost of treatment
- cost of death
- cost of sequelae/ disability

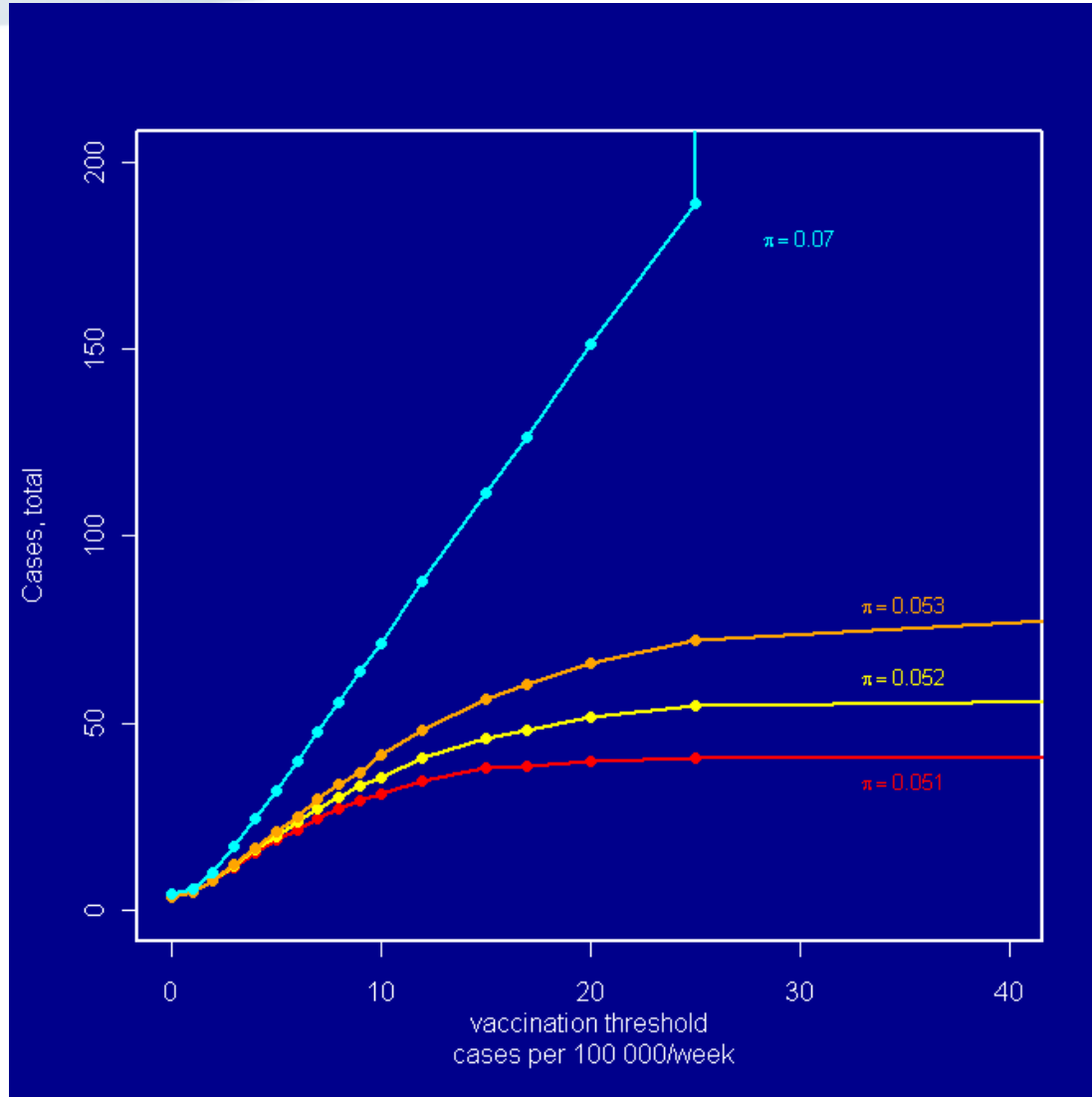


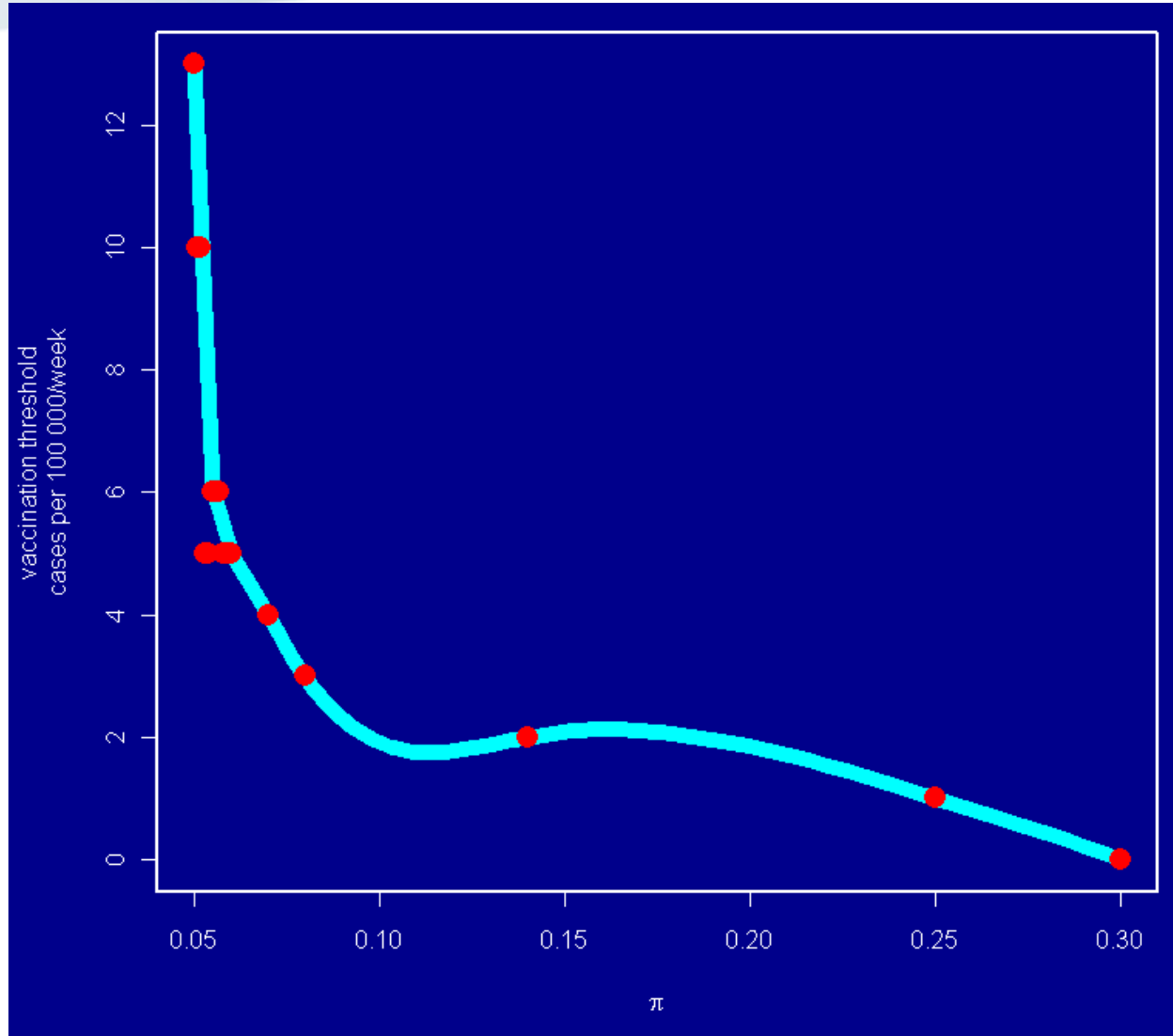
# Parametrization

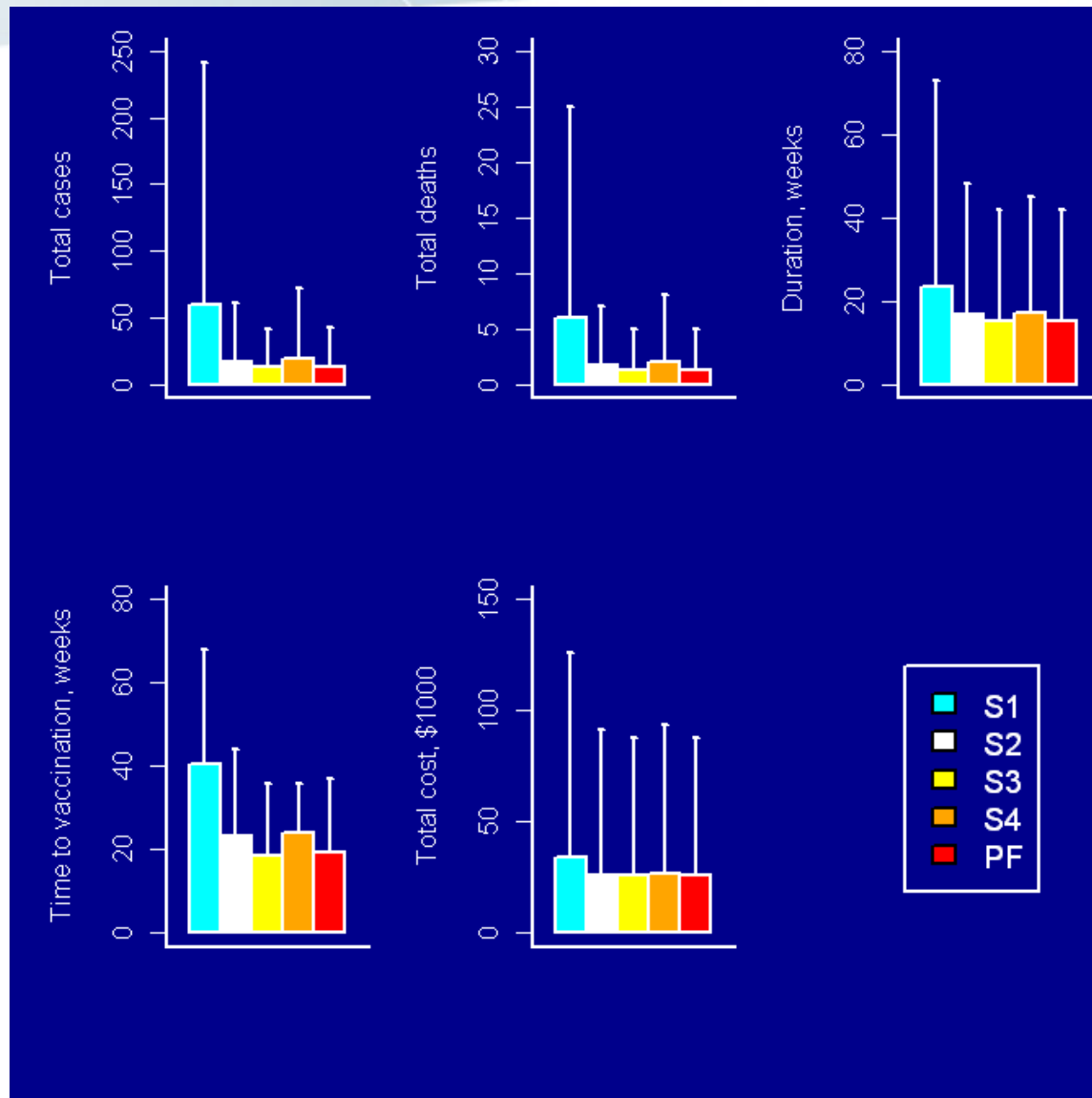
- 10% case-fatality within a week
- 2.5 weeks of recovery per infected person  
 $\Rightarrow \mu = .0265$  and  $\gamma = .2382$
- attack rate: 250-1000 per 100000
- duration: 30 weeks  
 $\Rightarrow N\pi \cong 0.26$
- number of contacts (const.)  $N=5$
- $n_0 = 100'000$ ,  $\pi \cong 0.05$ ,  $\alpha = 80\%$ ,  $\rho = 3\%$

# Response Scenarios









# Some Insights:

- The outcome of an epidemic is apparently highly sensitive to the values of the individual contagion probability  $\pi$
- The vaccination time is determined by the response strategy chosen: the less contagious the disease is assumed to be, the higher the optimal threshold and, consequently, the later the vaccination time.
- Setting the vaccination rules without reliable information on contagious probability increases the expected total costs
- Information on timing of the weather event is a major factor in the determination of the optimal vaccination response

# Discussion

- Carriage is not explicitly considered
- Homogeneous population is an oversimplification
- Dollars vs. Lives
- Endogeneous decision rules vs. Dynamic decision-making with a learning mechanism.